# The Crystal Structures of Two Compounds Found in Dental Amalgam: Ag<sub>2</sub>Hg<sub>3</sub> and Ag<sub>3</sub>Sn\*

BY C.W. FAIRHURST<sup>†</sup> AND J.B. COHEN

Department of Materials Science, The Technological Institute, Northwestern University, Evanston, Illinois, U.S.A.

(Received 27 January 1969 and in revised form 18 January 1971)

The structures of two of the three common compounds found in dental amalgam have been determined with single crystals. Intensity measurements were made with a diffractometer. The space group of Ag<sub>3</sub>Sn is *Pmmn*; the cell constants (determined with powders and a diffractometer) are a = 5.968 (9), b = 4.7802 (4), c = 5.1843 (9) Å. There are two formula weights per cell. Close packed layers, each containing an ordered array of Ag and Sn atoms, occur at  $b = \frac{1}{4}$  and  $\frac{3}{4}$ . No disorder was detected at temperatures below 175 °C. The weighted *R* value (on *F*) was 0.150. Ag<sub>2</sub>Hg<sub>3</sub>, although long considered to have the  $\gamma$ -brass structure (but with an unusual composition) is cubic with space group 123. The Hg atoms occupy general positions; vacancies of approximately 10% occur. There are 50 atoms per cell. The weighted *R* value (on *F*) was 0.187. Deformation markings are easily produced in Ag<sub>3</sub>Sn. The shear elements are:

$$K_1 = (0\overline{1}0), \qquad \eta_1 = [0\overline{1}\overline{1}]; \\ K_2 = (011), \qquad \eta_2 = [0\overline{1}1].$$

Intensity measurements from one such region indicate that the structure is the same as that of the unsheared crystal, indicating that these markings are true twins. Some growth twins were found in  $Ag_2Hg_3$ ; the composition plane appears to be (112).

#### Introduction

Dental amalgam is a multi-phase solid consisting of the  $\varepsilon$  phase, Ag<sub>3</sub>Sn, of the silver-tin system, the  $\gamma$  phase of the silver-mercury system, and the  $\gamma$  phase of the tin-mercury system. Some form of amalgam has been in use since about 1826 but the present form was first reported in 1895 (Black, 1895, 1896). A generalized equation for the amalgamation is given as (Ryge, Fairhurst & Fischer, 1961):

$$Ag_{3}Sn + Hg \rightarrow \gamma_{1}(Ag - Hg) + \gamma_{2}(Sn - Hg)$$
  
unreacted Ag\_{3}Sn . (1)

Previous studies (Fairhurst & Ryge, 1962) have identified and determined the structure of the Sn-Hg phase. The purpose of this investigation was to determine the crystal structures of the silver-tin and silvermercury phases.

Murphy (1926) studied the equilibrium conditions of the silver-tin binary system and established the existence of Ag<sub>3</sub>Sn. Preston (1926) described the structure as a close-packed hexagonal phase, but Hume-Rothery (1926) suggested that a multiple hexagonal cell would better satisfy the hexagonal symmetry and the composition requirements for Ag<sub>3</sub>Sn. X-ray diffraction from powder specimens (Nial, Almin & Westgren, 1931) showed that the structure of Ag<sub>3</sub>Sn was really a 'deformed' hexagonal close-packed structure; the orthorhombic lattice constants were reported as:

$$a = 2.98, b = 5.149, c = 4.771 \text{ Å}$$
.

As all of this work was based on powder patterns the true structure could have been missed if any weak peaks were present. This condition exists for certain 'deformed' hexagonal structures (Karlsson, 1951).

The silver-mercury  $\gamma$ -phase was reported to be a body centered cubic structure (Murphy, 1931; Preston, 1931) with a cell edge of 10·0 Å. Berman & Harcourt (1938) examined natural crystals (which they called 'Moschellandsbergite') and assigned the *Im3m* space group to this mineral. Their chemical analysis of these crystals indicated the composition to be Ag<sub>2</sub>Hg<sub>3</sub> and the density to be 13·48 g.cm<sup>-3</sup>, in agreement with Murphy (1931).

#### Experimental

## 1. Preparation of single crystals of Ag<sub>3</sub>Sn

Ag<sub>3</sub>Sn crystals were obtained by slowly cooling melts containing 58 at.% tin from 525 to 300°C (into the two-phase region Ag<sub>3</sub>Sn plus liquid), then quenching the melts to 25°C. The resulting ingots, containing about 50 vol.% of the Ag<sub>3</sub>Sn phase, were then placed in concentrated HCl for twenty-four to forty-eight hours with intermittent cleansing in detergent solution in ultrasonic cleaning equipment. A large number of small crystals were freed from the ingot in this manner. The crystals were relatively ductile and mechanical deformation was readily produced. The deformation markings were detected with optical microscopy, and extra Bragg reflections occurred when they were present.

<sup>\*</sup> This paper is taken from the Ph.D. thesis of one of the authors (C.W.F.), submitted in partial fulfillment of the degree requirements for Northwestern University, 1966.

<sup>&</sup>lt;sup>†</sup> Present address: General Manager, Dental Research and Development, S. S. White Division, Pennwalt Corporation, Philadelphia, Pennsylvania, U.S.A.

Care was taken to choose unmarked crystals for structural studies. Some crystallographic features of the deformation will be reported here.

## 2. Preparation of single crystals of $Ag_3Hg_3$

The silver-mercury y-phase forms at 127°C by a peritectic reaction. Attempts to obtain suitable crystals from melts, or by diffusion anneals within the solubility limits of this phase, were unsuccessful. Crystals were obtained by slowly cooling melts containing 0.3to 0.4 at. % silver in mercury. The melts were cooled from 110 to 30°C, through the liquid plus  $\gamma$ -phase region over a three-week period. The final temperature was maintained for five days. The majority of the excess mercury was removed by aspirating through a linen cloth. The crystals were quite brittle and hence could be ground in a Bond (1951) crystal grinder. Although resulting shapes were nearly spherical, slight imperfections were still evident which can be important in structural studies for such highly absorbing elements as silver and mercury. Occasionally, twinned crystals were found.

## 3. X-ray techniques

The diffraction symbols were obtained with a precession camera. Many of the actual films have been

## Table 1. Values of hkl and $\sin^2 \theta$ for Ag<sub>3</sub>Sn, copper K radiation 25°C

Specimen was -325 mesh powder annealed in argon at 300°C for 15.5 hours. Slow scans on a diffractometer were employed: peak positions were determined by bisecting horizonal lines and extrapolating to the profile. Wavelengths were those in International Tables for X-ray Crystallography (1962).

			Parameter Sta	indard deviati	on		
			a = 5.968  Å b = 4.7802 c = 5.1843	0·009 Å 0·0004 0·0009			
hkl	λ	Calculated $\sin^2 \theta$	Observed $\sin^2 \theta$	hkl	λ	Calculated $\sin^2 \theta$	Observed $\sin^2 \theta$
002 cř	α	0.0885	0.0881	611	<i>α</i> 1	0.6504	0.6512*
020 b	α	0.1039	0.1035	243	αı	0.6803	0.6789
012	α	0.1144	0.1142	440 a	α <sub>1</sub>	0.6814	0.6811
022	α	0.1924	0.1920	440 a	a	0.6847	0.6844
312	α	0.2645	0.2636	523	α <sub>1</sub>	0.7186	0.7200*
203	α	0.2653	0.2659	523	α2	0.7221	0,200
032	αι	0.3218	0.3216	424	αı	0.7233	0.7239*
223	αī	0.3690	0.3676	621	αı	0.7251	
104	21	0.3699	0.3696	424	27	0.7269	0.7262*
104	$\alpha_{2}$	0.3717	0.3718	621	α.2	0.7287	0.7301*
014	α <sub>1</sub>	0.3792	0.3785	334	α <sub>1</sub>	0.7365	0 / 0 0 1
412	α1	0.3806	0.3806	052	αı	0.7368	0.7367
014	α	0.3810	0.3816	334	α,	0.7401	0,000
330	αī	0.3833	0.3836	051	a2	0.7404	0.7404
040 b	$\alpha_1$	0.4150	0.4149	044	α1	0.7683	0.7680
040 <i>b</i>	$\alpha_2$	0.4171	0.4169	044	25	0.7721	0.7716
024	α1	0.4570	0.4566	006 c	$\alpha_1^-$	0.7947	0.7949
422	α	0.4584		006	α2	0.7987	
024 c	$\alpha_2$	0.4592	0.4592*	350	α1	0.7983	0.7981*
422	$\alpha_2$	0.4607	0.4620*	603	α	0.7979	
304	α1	0.2030		603	$\alpha_2$	0.8019	
042	α	0.5033	0.5033	135	α	0.8020	0.8013*
304	$\alpha_2$	0.5055		533	α	0.8483	
042	α2	0.2028	0.5056	235	α1	0.8520	0.8496
034	α1	0.5867	0.5865	541	α1	0.8533	
432	α1	0.2881		631	α1	0.8248	0.8543
034	α2	0.5896	0.5892	235	α2	0.8562	0.8558*
432	α2	0.5910	0.5927	541	α2	0.8575	0.8579*
503	α1	0.6148	0.6159*	631	α2	0.8590	0.8603*
404 a	$\alpha_1$	0.6195	0.6192*	026 c	α1	0.8985	0.8980
404 a	α2	0.6226	0.6226*	623	αι	0.9017	
513	α1	0.6408	0.6418	026	α2	0.9029	0.9026
414	α1	0.6455	0.6459	623	α2	0.9061	
414	α2	0.6487		702	α1	0.9039	0.9053*
530	α1	0.6496	0.6485	702 a	$\alpha_2$	0.9084	0.9097
530	α2	0.6528		060 b	$\alpha_1$	0.9338	0.9339
				$060 \ b$	<i>α</i> 2	0.9385	0.9385*

\* Peaks were low in intensity and poorly defined.

† Peaks labeled a, b, c were used to obtain corresponding lattice constants by plotting against Nelson-Riley function =  $\frac{1}{2}\left(\frac{\cos^2\theta}{\sin\theta}+\frac{\cos^2\theta}{\theta}\right)$ 

reproduced elsewhere (Fairhurst, 1966). Integrated intensities were obtained by counting at discrete  $2\theta$ positions through a peak in a  $\theta$ - $2\theta$  scan on a diffractometer. Care was taken to be sure the slits were open adequately to receive all of a peak, and the scan range was adjusted (for each peak) to be sure the background was reached. For Ag<sub>3</sub>Sn, Rh-filtered Ag radiation was employed, to maximize the difference between the scattering of Ag and Sn atoms (which differ by only three in their atomic number). For Ag<sub>2</sub>Hg<sub>3</sub>, Mo radiation was employed, and when integrated intensities were obtained, balanced filters of Y and Zr were used, expect for very weak peaks for which only the Zr filter was used. Corrections were made for background in all cases, from readings on either side of a peak.

Patterson projections, electron density maps and least-squares refinement were performed on a CDC 3400 computer using Professor J. Ibers's mapping program (FORDAP) and a least-squares program (Busing, Martin & Levy, 1960) respectively. The variance  $[\sigma^2(I)]$  of the intensity was calculated as (net counts)<sup>-1</sup>; except for peaks less than sixteen times the minimum value for which, following Hughes (1941),  $[16(net counts)]^{-1}$  was employed.

#### Results

## 1. Ag<sub>3</sub>Sn

Exposures on the precession camera of three to five days were employed so that any weak peaks whose intensity depended on the difference in scattering of Ag and Sn could be detected. Weak reflections were indeed found between rows of diffraction spots with constant h. From well annealed powders (see Table 1) the lattice parameters were found to be

a = 5.968 (9) A	١
b = 4.7802(4)	
c = 5.1843(9)	

The a value is twice that previously reported (Nial *et al.*, 1931).

The conditions for diffraction were:

$$(h00: h=2n)$$
  $(hk0: h+k=2n)$   
 $(0k0: k=2n)$ 

These conditions are consistent with either  $Pm2_1n$ (or  $P2_1mn$ ) –  $C_{2v}^7$  (No. 31), and  $Pmmn - D_{2h}^{13}$  (No. 59).

On the basis of reported density values (Nial et al., 1931) and the new lattice parameters, the unit cell of Ag<sub>3</sub>Sn contains eight atoms, six atoms of silver and two of tin. A trial model of the structure of Ag<sub>3</sub>Sn was deduced from qualitative considerations of packing of a close-packed structure, plus the fact that the 200 reflection was relatively weak whereas the 400 was very strong. This structure has a packing efficiency 97% of that for a fully close-packed structure based on the metallic radii of Ag and Sn and the volume of the cell. The weak diffraction from the (200) planes can be accounted for by planes at  $x = \frac{1}{4}$  and  $x = \frac{3}{4}$  which contain all silver atoms, whereas the alternative planes might contain half silver and half tin. Attempts to pack such layers in the noncentrosymmetric space group yielded a value for the c axis twice the measured value. Distortions of the layers for  $P2_1mn$  or  $Pm2_1n$  seem unlikely in view of the close-packed nature of the structure. Furthermore, hkl peaks with h odd were quite weak, which would not be the case for the noncentrosymmetric space groups. The Pmmn space group was therefore assumed to be the correct choice.

A crystal free of deformation markings, but possessing well-defined faces was chosen for collecting intensity data. (Its size was roughly 0.3 mm.) The Albrecht (1939) method was used to obtain absorption corrections, some 35,000 path-lengths being employed. One hundred and thirty-nine integrated intensities were measured and corrected.

From a ball model, trial atom parameters were

Table 2. Parameters for Ag<sub>3</sub>Sn (space group: Pmmn, No. 59)

				Origin Thermal paran	the at symmetry neters $\beta$ are m	center ultiplied by 10 <sup>.</sup>	4.			
Ag <sub>1</sub> Ag <sub>2</sub> Sn	Equipoint 4( <i>f</i> ) 2( <i>b</i> ) 2( <i>a</i> )	x 0.00 <sup>1</sup> / <sub>4</sub> <sup>1</sup> / <sub>4</sub>	y 14 34 14	z - 0·3369 (7) - 0·1723 (17) 0·1687 (13)	$\beta_{11} \\ 90 (10) \\ 110 (20) \\ 4 (10)$	$\beta_{22}$ 90 (20) 47 (25) 75 (25)	$\beta_{33}$ 100 (10) 127 (25) 70 (14)	$\beta_{12}$ 0 0 0 0	$\beta_{13} - 77 (15) = 0 = 0$	$\beta_{23}$ 0 0 0 0
		р <u>у</u>		ACT () ACT () ACZ () ACT () ACZ () AC						

Fig. 1. Stereo pair of the unit cell of Ag<sub>3</sub>Sn. [Drawn with ORTEP (Johnson, 1965)].

obtained. Least-squares refinement was carried out calculating both the residual indices

$$R_{1} = \frac{\sum_{i} (F_{i}^{obs} - F^{calc})}{\sum_{i} F_{i}^{obs}}$$

and

$$R_2 = \begin{bmatrix} \sum_{i}^{N} w_i (F_i^{\text{obs}} - F_i^{\text{calc}})^2 \\ -\sum_{i}^{N} w_i (F_i^{\text{obs}})^2 \end{bmatrix}^{\frac{1}{2}}$$

where  $w_i$  is a weight factor based on the variance of the measured intensities for each peak,  $w_i = 1/\sigma(I)^2$ . Refinement was on  $R_2$ . The scattering factors employed were those calculated by Cromer & Waber (1965) with corrections for anomalous scattering (Cromer, 1965). Anisotropic temperature factors were employed. Equivalent peaks were averaged; also some peaks (such as hol with h odd) which were only barely detected after long exposures on the precession camera, were not found with the relatively short times for the scans on the diffractometer. Some 55 reflections remained for the refinement.

The structure refined to an  $R_1$  value of 0.109, using anisotropic thermal parameters and an  $R_2$  of 0.150. Refinements with isotropic temperature factors gave  $R_1 = 0.119$ ,  $R_2 = 0.180$ . The final parameters are given in Table 2, and the structure factors in Table 3. The

Table 3. Observed and calculated structure factors for Ag<sub>3</sub>Sn

ĸ	L	FO	FC					
*****	н	- 0	*****	*****	н		4	*****
0	2	6519	8882	٥	0	114	441	13045
0	4	4943	5686	ō	ź	65	542	5809
ō	5	2232	1045	õ	3		551	545
ō	6	6714	7110	0	4	4	518	4296
Ó	8	2390	2212	ō	6	6	078	5965
ō	10	1237	1283	0	8	- 10	329	1950
ō	12	1127	1419	0	10	1 3	370	1232
i	1	713	538	4	0	9	166	8595
ź	ō	19053	17456					
2	2	9369	7433					
3	3	599	741	*****	н		6	*****
4	0	11083	11351				•	
4	4	5281	3875	0	2	1	147	697
6	0	8219	7447	0	3	76	85	7439
6	6	4873	4124	0	9	2	753	2794
8	0	5233	4933					
8	8	1501	1013	*****	н	-	8	*****
10	0	3013	3160					
12	0	1595	1886	0	0	66	98	6073
				٥	2	- 34	63	2892
*****	н	= 1	*****	0	4	24	32	2456
				0	6	40	98	3929
0	1	383	389	0	8	15	41	1406
0	2	533	606	0	12	12	61	1238
0	5	532	493	8	0	31	19	2618
*****	н	• 2	*****	*****	н	•	10	*****
0	0	483	454	0	5	13	48	1679
0	1	8113	8859				-	
0	2	755	834	*****	н		12	*****
0	3	11994	12990					
0	4	709	639	0	0	29	90	2981
0	5	4971	4270	0	6	20	12	2250
0	7	2882	2689					
0	8	707	752					
2	0	486	517					
*****	н	- 3	****					
0	1	433	407					
ō	2	447	428					
3	ō	499	522					

structure is shown in Fig. 1. Some typical interatomic distances are given in Table 4.

Table 4. Characteristic distances in Ag<sub>3</sub>Sn

Ag(1)-Ag(1) [56405]	2·928 Å
Ag(1)-Ag(1) [55502]	2.984
Ag(1)-Ag(2) [55501]	2.944
Ag(1)-Ag(2) [56405]	2.950
Ag(1)-Sn [56505]	2.949
Ag(1)-Sn [55401]	2.966

\* The first atom is in the first position of the rank 8 equipoint of Pmmn (No. 59). Other positions are indicated as in ORTEP (Johnson, 1965). The symbol in square brackets is:

(5 + x unit cell translations).  $10^4 + (5 + y \text{ translations})$ .  $10^3 + y$ (5 + v translations).  $10^2 + (\text{number of coordinate set in general})$ equipoint). The last value is the number of the coordinate set reading left to right in International Tables for X-ray Crystal*lography* (1952).

Murphy (1926) reported a change in resistivity of Ag<sub>3</sub>Sn at 60°C which might be due to disordering. Precession photographs were taken with Polaroid film, with the specimen heated by hot argon to 25, 105 and 175°C. No change in the weak reflections was observed.

## 2. Twinning in Ag<sub>3</sub>Sn

Occasional deformation markings were first identified by two-surface analysis, measuring the angle between the two surfaces with an optical goniometer. [The surfaces were identified as (001) and (101) planes by diffraction.] The plane of the markings  $(K_1)$  was (011). The tilt between the (001) face and a marking was  $5.5^{\circ}$  and that between a marking and the (101) face was  $5 \cdot 3^{\circ}$ . With these tilts, a stereographic analysis was performed assuming the marking was due to simple shear, to obtain the shear direction  $(\eta_1)$  (Greninger & Troiano, 1949).  $\eta_1$  was [011]. Precession photographs of crystals with markings were taken of the (100)\* plane which is parallel to the 'plane of shear' – the plane perpendicular to  $K_1$  and containing  $\eta_1$ . As many as twenty extra spots were observed, all of which were reflections (across the trace of  $K_1$  in this plane) of spots in crystals without markings. This strongly suggested that the specimen was twinned. Accordingly, by trial and error the second undistorted plane in a simple shear  $(K_2)$  was located. The trace of this plane in  $K_1$  must be perpendicular to  $\eta_1$  and its position before and after shear must be symmetrically located with respect to the normal to  $K_1$ . Furthermore, as  $\eta_1$  and  $K_1$  are rational,  $K_2$  must be as well (Cahn, 1954). One plane that satisfied these conditions was (011).  $\eta_2$ , the second undistorted line, must lie in  $K_2$ and be perpendicular to the line of intersection of  $K_2$ and  $K_1$ ;  $\eta_2$  is then [011]. The shear (s) is:

### $s = 2 \cot 85 \cdot 2^\circ = 0.168$

where  $85 \cdot 2^{\circ}$  is the angle between  $K_1$  and  $K_2$ . The shearing process is indicated by Fig. 2 from which it can be seen that:



Fig. 2. (a). Relative positions of atoms before and after twinning in Ag<sub>3</sub>Sn. Stars are Ag atoms, squares are Sn. Arrows indicate total movement of atoms. Initial positions prior to shear and shuffles are indicated by filled symbols. Final positions are open symbols. (b) Plane of shear; unit cell corners indicated by dots. The angles  $\gamma$ ,  $\alpha$ ,  $\beta$  are shown.

(a) atoms must 'shuffle' in directions other than the shear direction if the product is to be a twin. Otherwise a new structure is generated by the shear, with b and c axes interchanged. Intensity data for 002, 004, 006, 020, 040, 060 from an untwinned crystal and a twinned crystal agreed; particularly the 006 was similar in intensity to the 004, whereas the 060 was much weaker than the 040. If no 'shuffles' had occurred the 060 would be similar in intensity to the 004, lese Fig. 2(a).]. The structure within a deformation marking is a twin.

(b) A simple check that  $K_2$  was correctly chosen can be obtained by measuring the angle  $\gamma$  [Fig. 2(b)] between diffraction from 00/ in a crystal and 0k0 in its twin; with the known cell constants the angle  $\gamma$  was calculated to be 4.4°. The measured angle was 4.7°. It is somewhat surprising that twinning and not a new structure is generated by shear, in view of the fact that large 'shuffles' are involved to maintain the ordered arrangement. It has been predicted in such cases that a new structure is expected (Laves, 1952). However, it is worth pointing out in this regard that simple shears in the **b** and **c** directions on a hard sphere model will carry out the entire atomic rearrangement without shuffles (Fairhurst, 1966).

In the Introduction it was pointed out that the unit cell is pseudo-hexagonal. In hexagonal indices, the twin plane is (1012) which is a common  $K_2$  for twinning in hexagonal metals (Rosenbaum, 1964).  $K_2$  in Ag<sub>3</sub>Sn is  $K_1$  in hexagonal metals. The magnitude of the shear is also comparable.  $\eta_1$  and  $\eta_2$  are not, however, equivalent.

## 3. $Ag_2Hg_3$

Precession photographs taken at 90° intervals around  $\langle 100 \rangle$  axes confirmed that the structure is cubic. The symmetry of the cube axis was twofold; thus, the Laue symmetry was m3. Extinctions were found only for h+k+l= odd. There were four possible space groups:  $I23-T^3$  (No. 197),  $I2_13-T^5$ (No. 199),  $Im3-T_h^5$  (No. 204), and  $Ia3-T_h^7$  (No. 206). The *Ia3* space group could be eliminated as the reflections observed included 013, 017, 015, etc., which are not allowable in this case. The chemical analysis of this phase, as indicated by Murphy (1931) suggests the compound is Ag<sub>2</sub>Hg<sub>3</sub>. The density was reported as 13.48 g.cm<sup>-3</sup>. Using a lattice parameter of 10.0 Å, the number of atoms per unit cell is about fifty. Intensities from the near-spherical crystal corrected

Table 5. Structural parameters ( $\times 10^4$ ) for Ag<sub>2</sub>Hg<sub>3</sub> (space group: I23 No. 197)

	Equi-	Occupation			Temperature factors							
	point	factor	Х	Y	Z	$\beta_{11}$	$\beta_{22}$	$\beta_{33}$	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$	
Hgı	(c)	8	1151 (7)	1151	1151	38 (5)	38	38	6 (5)	6	6	
Agi	(c)	8	3285 (10)	3285	3285	9 (5)	9	9	3 (6)	3	3	
Hg <sub>2</sub>	(f)	$22 \cdot 2$ (1:1)	2957 (6)	3359 (7)	291 (6)	16 (4)	50 (6)	23 (5)	-4 (4)	-5(3)	-11 (4)	
Ag <sub>2</sub>	( <i>d</i> )	12	3550 (15)	0	0	23 (10)	32 (10)	17 (9)	0	0	3 (12)	

for absorption\* were used to prepare a three-dimensional Patterson function. The sections containing significant Patterson peaks were z=0.0, 0.175, 0.325. For  $I2_13$  there are not proper equipoints to distribute the 30 atoms of Hg and 20 atoms of Ag to obtain an ordered structure. For ordered structures in *Im3* and I23 the 20 Ag atoms must be distributed in such a way that vectors at  $\frac{1}{2}$ ,  $\frac{1}{2}$ , 0 or  $\frac{1}{2}$ , 0, 0 are required in the Patterson synthesis. These were absent.

It has long been thought that this material was a ybrass type in view of the large cubic cell and the electron-to-atom ratio of 1.6. Many of these compounds contain 52 atoms in a unit cell, but it is not unusual for such structures to have vacant sites (Betterton & Hume-Rothery, 1952). Hence, the possible space groups were reconsidered with 32 Hg sites per cell, two of which are vacant and chosen at random from cell to cell. (If 22 Ag and 30 Hg atoms are considered, reasoning similar to that in the previous paragraph eliminates this possibility.)  $I2_13$  and Im3 were still not possible. The only possible space group was I23 with Hg atoms on 24(f) and 8(c) equipoints and Ag on 12(d) and 8(c). The atomic coordinates are:

 $(0,0,0; \frac{1}{2}, \frac{1}{2}, \frac{1}{2}) + 24(f): x, y, z; z, x, y; y, z, x; x, \bar{y}, \bar{z}; z, \bar{x}, \bar{y}; y, \bar{z}, \bar{x} \\ \bar{x}, y, \bar{z}; \bar{z}, x, \bar{y}; \bar{y}, z, \bar{x}; \bar{x}, \bar{y}, z; \bar{z}, \bar{x}, y; \bar{y}, \bar{z}, x \\ 12(d): x, 0, 0; 0, x, 0; 0, 0, x; \bar{x}, 0, 0; 0, \bar{x}, 0; 0, 0, \bar{x} \\ 8(c): x, x, x; x, \bar{x}, \bar{x}; \bar{x}, x, \bar{x}; \bar{x}, \bar{x}, x.$ 

 $I\overline{4}3m - T_d^3$  (No. 217), the space group for the structure having the *Strukturbericht* designation  $D8_2(Cu_5Zn_8)$ , is a typical  $\gamma$ -brass type. The rank 24 equipoint in this case has the form xxz rather than xyz for 123. Both groups are noncentrosymmetric. The 411 and 330 peaks are strong reflections from Ag<sub>2</sub>Hg<sub>3</sub> as for the known D8<sub>2</sub> structures. For all these reasons, it was decided to refine the structure using as starting parameters atomic coordinates for Cu<sub>5</sub>Cd<sub>8</sub> (Bradley & Gregory, 1931). Again atomic scattering factors were corrected for dispersion (Cromer, 1965; Cromer & Waber, 1965).

\*  $\mu r$  was taken to be 14, by averaging the radius at several points, and the corrections for a sphere in *International Tables* for X-ray Crystallography (1959) were employed.



After initial stages of refinement, equivalent reflections were averaged and those that had intensities less than three standard deviations were eliminated, reducing the number of independent reflections from 231 to 160. Refinement was continued with isotropic and anisotropic temperature factors. In both cases, the occupation of the Hg 24(f) equipoint was a variable. With anisotropic factors  $R_1$  was 0.143,  $R_2$ was 0.187; for isotropic temperature factors,  $R_1 = 0.160$ ,  $R_2 = 0.208$ . Results are given in Table 5 for the anisotropic factors, and the structure factors are given in Table 6. Note that there are about two vacant Hg sites on the rank 24 equipoint; with the error on this value it is barely significant, but is supported by the reported density and lattice parameter; as mentioned earlier, these lead to 50 atoms per cell.

[Baird & Muller (1969*a*) have attempted to refine our data using an orthorhombic structure but found that the resulting parameters were cubic, further sup-

Table 6.	Observed	and	calci	ulated	structure	factors
		for	Ag <sub>3</sub> l	−lg₃		

••••	• н	• •	•••••		•	• •	•••••		• н	• •	•••••		H + 10	
2	2	4159	4859		4	15753	13002	4	ć	205	7 3119	2	0 3580	3480
3	3	+1328	37688	2	4	3835	3972		2	85.91	9 7925		8451	8979
•	0	1659	2865		0	A723	4320		Ż	1327.	9888		185	2205
			4197	6	٥	5396	6067			10.1	3028	10	1100	24.85
	0	22083	20170	8	¢	2353	1952			912	79.66			2007
	- 2	14414	11001	8	2	3596	4194				1469	10	0 2 0 0	2011
ž		20013	13003	15	ō	8551	8931				2009	10 1	5 52 57	5311
	- 1		2020	12	ō	5833	6205					10 11	0 2493	2500
		4434		12	5			12	•	1.0	•	12	0 2177	2257
		2040	5450	14	6	5803	6813							
10	. 0	2099	5321	• •	•							*****	4 - 11	
10	10	1856	1955					****	• •	•				
11	11	+6+6	4377		^	• ,						1 1	0 1443	1589
12	0	2596	2510				A 1		٥	6584	6785	5 1	0 5729	5492
14	0	2452	2478		÷.	10112	9242	,	0	3675	3753	9.	2118	1577
1 🖷	14	1563	2318	,	•	2001	2220	\$	- a	8648	7291	11 .	2 1816	937
						15803	16422	;	5	612	5 344		3574	2700
	• н	• 1		,	۰	1337	1512	,		17491	12672	11 1	5798	0.010
				1	٥	4014	3710	;		21.00		11 I.	1756	2028
1		15137	16986	•	٥	4256	4315	;		6979	6 177			
ż	3	7578	9178	12	3	1307	2249				3714	., .,	1437	1211
- ž	5	4808	5928										. 12	
3	ō	2233	3116		N	• •	*****	19		101				
- ŝ	- 2	3795	5029									, ,		+001
ñ		4505	4112	2	٥	9707	12+21		• •		,			
	- i		\$470	•	2	10667	6683							2047
1	÷.	14.1		•	٠	29966	21970	4	0	4121			1040	
		11047	1 3 6 3 6			3839	2073	•	0	1761	2147	14 1	2898	2000
1	Š				۰	3608	3878	6	0	4335	a 115	14 1	• • • • • • •	4/60
2	1	0402	6705	6	õ	56.58	.139	8	2	3959	3040			
2	•	4414			ō	8260	7565	8	•	2571	2176		13	
		3034		1.	ň	6360	6076		•	239	2272			
		0481	7436	• ·	•			8		9701	8774	1 1	5408	5045
•	•	4980	3/43		~			8	10	202	2038	, ,	2340	3439
2	°.	7964	7991			- /		10	0	628	5229	7 1	0 9035	5411
	~	9891	10652		~		1.01	12	0	278	2840	13 1	- 2696	2816
1	•	13825	13864				3047	1.	0	190.	2 3230	13 (	5 2063	2618
8	1	4557	\$007	2	ÿ		1193					13 1.	2 1500	2056
8	3	8572	7843	2	4	7631	0090		• •			15	0 1400	2318
8	•	1774	1935	2	٠.	4614	3606							
9	0	2833	685	2	•	3160	2723	1	0	10355	10188		4 * 14	
9	٠	4815	4737	,		7527	1741		n	A150				
10	1	10561	9452	<b>.</b> .	10	3057	3036	;		114	2816	2	2734	3026
10	ż		4813	,	0	8159	5694	÷	ž		3413		2889	2928
11	ò	4140	3802	9	0	12293	9453		- 1		A 119	a	2705	3030
12	ī	3600	3115	10	5	3126	3036		- 2	284	2,90	10	2747	2754
12	-	3052	1794	11	0	6875	5980					12	3713	1820
13		1.4.7.4	1834	13	٥	80+5	7610			310	43/6			
11	ÿ	4197	41122	15	ò	1954	2508	2	10	1+3	1425			
11	1	5036							- 44	136	5 2292		- 13	
14	-	2814	1246					13	0	\$70	2834			
1.	;	A200	4004									1		
		2000	3.0.									· ·	0 3080	+ >>1
••														





porting the space group we have chosen. They also tried a least-squares refinement for the cubic space group used here, I23, but used only unit weighting, no corrections for anomalous dispersion, and also appear to have chosen the wrong equivalences (due to symmetry) of the anisotropic temperature factor for the Ag atoms on the 12(d) equipoint.]

The unit cell is shown in Fig. 3. The lattice parameter employed was 10.0506 Å for Hg-rich Ag<sub>2</sub>Hg<sub>3</sub> (Dreiner, 1958). Some typical interatomic distances are given in Table 7.

Table	7.	Nearest-neighbor	• distances	in	Ag <sub>2</sub> F	Ig.
					4 7 4.	4 3.1

Hg(1)-Hg(1) [55504]	3·272 Å
Hg(2) - Hg(2) [55521]	2.936
Hg(1)-Hg(2) [55501]	2.994
Hg(1)-Ag(1) [45516]	2.990
Hg(1)–Ag(2) [55501]	2.914
Hg(2)-Ag(1) [55422]	2.890
Hg(2)-Ag(2) [55518]	2.880
Ag(1)-Ag(2) [55517]	3.057
Ag(2)-Ag(2) [65507]	2.915

\* The first atom is in the first position of the equipoint. The second position is indicated as in *ORTEP* (Johnson, 1965). The symbol represents  $(5+x \text{ unit cell translations}) \cdot 10^4 + (5+y \text{ translations}) \cdot 10^3 + (5+z \text{ translations}) \cdot 10^2 + (number of coordinate set in general equipoint). The last term is obtained by counting from left to right in the positions given in the text.$ 

There are two interesting features of this structure: (i) The majority of the heavy mercury atoms are in general positions. The result of this is that the structure has only twofold symmetry along the cube axis instead of the fourfold in the  $D8_2$  structures of  $Cu_5Zn_8$ and  $Cu_5Cd_8$ ; (ii) the total electron count for all the atoms in the cell is about 76, lower than the values of 84–88 usually found for such compounds. (It should be kept in mind that the crystals were prepared from Hg-rich solid solutions, so that the electron count would be the highest over the range of compositions for which this phase exists.)

### 4. Twinning in Ag<sub>2</sub>Hg<sub>3</sub>

Some extra reflections were found for certain crystals grown at room temperature, which appeared to be reflections of other spots across (112) planes. A similar twinning has been detected by Baird & Muller (1969b) in crystals grown from nitrate solutions.

#### Discussion

A new unit cell was detected for  $Ag_3Sn$ . The structure is ordered and remains so until at least 175 °C. This phase deforms mechanically, and intensity data show that observed shear markings are true twins, despite the ordered arrangement of atoms. The structure can be described as deformed hexagonal similar to structures with the *Strukturbericht* designation  $DO_{22}$ . It has the same structure as Cu<sub>3</sub>Ti (Laves & Walbaum, 1939; Karlson, 1951), and Mo<sub>3</sub>Ni (Saito & Beck, 1959). In all these phases nearly close-packed layers are stacked along a pseudo threefold axis (the *b* axis), in a h.c.p. sequence, *abab*.... The layers themselves consist of  $\langle 100 \rangle$  rows of atoms, alternating rows being all Ag or half Ag-half Sn, as can be seen in Fig. 1. It is interesting to note that all of these phases reported previously have involved one or more transition elements, whereas Ag<sub>3</sub>Sn does not. The pseudo-hexagonal nature of the structure also expresses itself in its twinning mode, which is similar to that for hexagonal metals.

The similarity of the structure of  $Ag_2Hg_3$  to that of the  $\gamma$ -brass type,  $D8_2$ , has already been pointed out. The reduced symmetry of the general position as compared to  $D8_2$  may be due to the vacant sites in the structure of  $Ag_2Hg_3$ .

This work was supported by the Advanced Research Projects Agency through Northwestern University's Materials Research Center under Contract SD-67 and through training and research grants DE22 and DE01057 from the National Institutes of Health-National Institute for Dental Research, and the Division of Research Facilities and Resources of NIH. Mr Robert Grosso performed the calculations of the absorption factor for Ag<sub>3</sub>Sn. Mr John Dunn and Miss Kirsti Paavola carried out the final stages of refinements as part of advanced courses in diffraction at Northwestern University.

#### References

- ALBRECHT, G. (1939). Rev. Sci. Instrum. 10, 221.
- BAIRD, H. W. & MULLER, F. A. (1969a). J. Biomed. Mater. Res. 3, 375.
- BAIRD, H. W. & MULLER, F. A. (1969b). J. Biomed. Mater. Res. 3, 369.
- BERMAN, H. & HARCOURT, G. A. (1938). Amer. Min. 23, 761.
- BETTERTON, J. O. & HUME-ROTHERY, W. (1952). J. Inst. Met. 80, 459.
- BLACK, G. V. (1895). Dent. Cosmos, 37, 553, 637.
- BLACK, G. V. (1896). Dent. Cosmos, 38, 43, 965.
- BOND, W. L. (1951). Rev. Sci. Instrum. 22, 344.
- BRADLEY, A. J. & GREGORY, C. H. (1931). Phil. Mag. 12, 143.
- BUSING, W. R., MARTIN, K. O. & LEVY, H. A. (1960). ORFLS. Report ORNL-TM-305, Oak Ridge National Laboratory, Tennessee.
- CAHN, R. W. (1954). Advanc. Phys. 3, 363.
- CROMER, D. T. (1965). Acta Cryst. 18, 17.
- CROMER, D. T. & WABER, J. T. (1965). Acta Cryst. 18, 105.
- DREINER, R. (1958). Thesis, Facultät für Bergbau and Hüttenwesen, Aachen, Germany.
- FAIRHURST, C. W. (1966). Ph. D. Dissertation, Northwestern Univ.
- FAIRHURST, C. W. & RYGE, G. (1962). Advanc. X-ray Anal. 5, 64.
- GRENINGER, A. B. & TROIANO, A. R. (1949). *Trans. A.I.M.E.* 185, 590.
- HUME-ROTHERY, W. (1926). J. Inst. Met. 35, 127.
- HUGHES, E. W. (1941). J. Amer. Chem. Soc. 63, 1737.

- International Tables for X-ray Crystallography, (1959). Vol. II, Birmingham: Kynoch Press.
- International Tables for X-ray Crystallography, (1962). Vol. III. Birmingham: Kynoch Press.
- JOHNSON, CARROLL K. (1965). ORTEP. Report ORNL-3794 Oak Ridge National Laboratory, Tennessee.
- KARLSSON, N. (1951). J. Inst. Met. 79, 391.
- LAVES, F. (1952). Naturwissenschaften, 30, 546.
- LAVES, F. & WALBAUM, H. J. (1939). Naturwissenschaften, 27, 674.
- MURPHY, A. J. (1926). J. Inst. Met. 35, 107.

- MURPHY, A. J. (1931). J. Inst. Met. 46, 507.
- NIAL, O., ALMIN, A. & WESTGREN, A. (1931). Z. Phys. Chem. B14, 81.
- PRESTON, G. D. (1926). J. Inst. Met. 35, 118, 129.
- PRESTON, G. D. (1931). J. Inst. Met. 46, 522.
- ROSENBAUM, H. (1964). *Deformation Twinning*. p. 43. New York: Gordon & Breach.
- RYGE, G., FAIRHURST, C. W. & FISCHER, C. M. (1961). Int. Dent. J. 11, No. 2.
- SAITO, S. & BECK, P. A. (1959). Trans. A.I.M.E. 215, 938. WILSON, A. J. C. (1942). Nature, Lond. 150, 152.

Acta Cryst. (1972). B28, 378

## The Crystal Structure of 4-Carbethoxyanilinium Bis-p-nitrophenylphosphate

#### By J. PLETCHER AND M. SAX

Biocrystallography Laboratory, Veterans Administration Hospital, Pittsburgh, Pa. 15240, U.S.A.

# and C. S. Yoo\*

Department of Crystallography, University of Pittsburgh, Pittsburgh, Pa. 15213, U.S.A.

## (Received 16 April 1971)

The crystal structure of a 1:1 complex between 4-aminobenzoic acid ethyl ester and bis-*p*-nitrophenylphosphate has been determined. Crystals are orthorhombic,  $Pna2_1$ ,  $a=12\cdot273$  (4),  $b=27\cdot357$  (4), c=7·114 (4) Å, Z=4. The intensities of 2221 reflections were measured with a four-circle automated diffractometer using Cu K $\alpha$  radiation. The structure was refined to an R of 0.049 over all the reflections. In the complex the 4-amino group is protonated. All three of the amino hydrogen atoms participate in hydrogen bonds to the phosphate group with N---O distances of 2.754, 2.780, and 2.838 Å. The bis*p*-nitrophenylphosphate ion, which is also found in crystalline complexes with phenacaine and procaine, has a CO-P-OC valency angle of 97.8°. This structural feature, along with the torsion angles about the phosphate ester bonds, shows greater similarity to that in the phenacaine complex. The molecular packing indicates that the nonpolar interactions between the components of the complex are more extensive than was observed in the procaine complex. This aspect was also apparent in the structure of the phenacaine complex, although not to the same extent as in the present structure.

#### Introduction

On the basis of studies with model systems (Feinstein, 1964; Feinstein & Paimre, 1966), Feinstein and Paimre suggested that local anesthetics block nerve conduction by complexing with phospholipids in the neural membrane. Their studies demonstrated that the local anesthetics would precipitate phospholipids or phosphodiester compounds in general. In fact, the reaction with a simple phosphodiester, bis-p-nitrophenylphosphate, resulted in the precipitation of a crystalline complex. To examine the nature of this interaction, we determined the crystal structures of several of these complexes (Sax, Pletcher & Gustaffson, 1970; Sax, Pletcher, Yoo & Stewart, 1971). The results of these structure analyses, along with other experimental observations, led to the suggestion that the hydrogenbond donor capability of local anesthetics was an important aspect in the anesthetics' mode of action (Sax & Pletcher, 1969). In exploring this idea further, we attempted to prepare a complex with a neutral, nonionizable local anesthetic. Benzocaine, which is 4-aminobenzoic acid ethyl ester, was selected for this purpose as it is normally regarded as a neutral, nonionizable drug. Contrary to expectation that the benzocaine complex with bis-*p*-nitrophenylphosphoric acid would exist in the uncharged or neutral form, crystalstructure analysis shows that the complex crystallizes in the ionized form.

## Experimental

Crystals of the complex were prepared by mixing equimolar solutions of bis-*p*-nitrophenylphosphoric acid\* and benzocainet in absolute methanol. White needle-shaped crystals of the complex were obtained

<sup>\*</sup> In partial fulfillment of the requirement for the Ph.D. degree.

<sup>\*</sup> Aldrich Chemical Company.

<sup>†</sup> Eastman Organic Chemicals.